

## Propositional and Predicate Logic – First Homework

The deadline for the homework is November 10, 2017 at 23:55 (11:55 pm). You can either hand me the solution on paper (preferably after the lecture on Nov. 9), or send it via e-mail to `Martin.Pilat@mff.cuni.cz` (a scan/photo of your handwriting is OK).

The points obtained for this homework count towards the points required to obtain the credit for the seminar.

1. Transform the formula  $((p \rightarrow \neg q) \rightarrow \neg r) \rightarrow \neg p$  into the conjunctive normal form and into the disjunctive normal form. **[0.5 points]**
2. Prove the formula  $(p \vee (q \wedge r)) \rightarrow ((p \vee q) \wedge (p \vee r))$  using the tableau method. **[0.5 points]**
3. Let  $T = \{p \vee \neg q, s \rightarrow q, r \rightarrow \neg(p \vee q)\}$  be a theory over  $\mathbb{P} = \{p, q, r, s\}$ . Count the number of non-equivalent formulas  $\varphi$ , such that  $T \not\vdash \varphi$ . **[0.5 points]**